Seismic analysis of lock–soil–fluid systems by hybrid BEM–FEM

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Abstract

A study of soil–structure–fluid interaction (SSFI) of a lock system subjected to harmonic seismic excitation is presented. The water contained lock is embedded in layered soils supported by a half-space bedrock. The ground excitation is prescribed at the soil–bedrock interface. The response is numerically obtained through a hybrid boundary element (BEM) finite element method (FEM) formulation. The semi-infinite soil and the fluid are modeled by the BEM and the lock is modeled by the FEM. The equilibrium equation for the lock system is obtained by enforcing compatibility and equilibrium conditions at the fluid–structure, soil–structure and soil–layer interfaces under conditions of plane strain. To the authors’ knowledge this is the first study of a lock system that considers the effects of dynamic soil–fluid–structure interaction through a BEM–FEM methodology. A numerical example and parametric studies are presented to examine the effects of the presence of water, lock stiffness, and lock embedment on the response.

Keywords: Seismic analysis; Boundary element method; Finite element method; Soil–structure–fluid interaction

1. Introduction

Seismic analysis of large systems considering soil–structure–fluid interaction (SSFI) result in a rather involved mathematical treatment when factors such as unbounded extent of soil and fluid, compressibility of water, geometry of structure, surface waves of water, and flexibility of structure, are taken into account. Systems that SSFI should be considered include: (1) submerged or off-shore; (2) dam–reservoir–soil; (3) storage tank; (4) intake towers; and (5) lock and dam. Chen [1] has given a review on the research up to 1982 of submerged off-shore systems. Developments on this topic can be found in Refs. [2,3]. A comprehensive review of the analysis of a dam–reservoir–soil system has been presented by Dominguez et al. [4]. Research covering different types of dam–soil–reservoir systems has been reported by Refs. [5–11].

In this study, the lock system is a fluid contained open-channel structure embedded in layered soil, see Fig. 1. It presents many similarities with a storage tank system, although the storage tank system is usually placed above the ground level and contains a bounded amount of fluid. A discussion on storage tank systems has been given by Antes and Latz [12]. In the early stage of studying the seismic response of storage tank systems, the tank was assumed to be rigid and anchored to a rigid base, e.g. Ref. [13]. Realizing that the flexibility of the tank can play an important role on the seismic response, later methods tried to address the issue. Representative semi-analytical procedures employ assumed modes and added masses to describe the displacement of the tank and account for the effect of the fluid–structure and SSFI. Representative works on the topic include Refs. [14–23]. A recent work [24] on the seismic response of towers and intake towers studies the effect of partial separation of the foundation from the soil and presents a review on pertinent topics including literature on the effects of soil–structure and SSFI.

As an alternative method, the finite element method (FEM) has found its application on the seismic analysis of storage tank systems. One of the primary advantages of FEM over semi-analytical procedures is that it is not limited to simple geometry structure. Edwards [25] is known to be the first to introduce FEM to SSFI. Other early studies are presented in Refs. [26–28]. In all these studies, the tank is assumed to be rigidly connected to the soil. A representative study [29] investigates the behavior of unanchored and flexible tanks.

A well documented disadvantage of FEM is its difficulty in modeling the semi-infinite soil and fluid domains. However, combination of the boundary element method (BEM) and FEM can overcome this difficulty. Although a large number of papers have been published on the...
application of BEM or FEM/BEM on the seismic analysis of systems considering soil–structure interaction (SSI), very limited studies can be found in the literature, where issues of soil–structure–fluid interaction (SSFI) are addressed. Two early applications of BEM to structure–fluid interaction (SFI) of fluid contained tanks appeared in 1980. In these studies the tanks are modeled by FEM and the incompressible fluid domain by BEM [30,31]. Koh et al. [32] have studied the dynamic response of storage tanks by combining BEM with the FEM. In all these works, no soil–structure interaction is considered. Therefore, they can be more properly classified as structure–fluid interaction (SFI), not SSFI problems. To the authors’ knowledge, one of the first investigations to include soil–structure–fluid interaction was Ref. [33]. In a paper by Antes and Latz [12], the SSFI is studied in the frequency domain by the so-called BEM–FIS method. In their work, the compressibility of fluid and surface sloshing is also included, and the SSFI is considered by attaching a flexible tank to a rigid foundation supported by an elastic soil.

The structural system studied in this work is a lock system supported by a layered soil, see Fig. 1. The SSFI is treated by a hybrid FEM/BEM in the frequency domain. Plate elements are employed to model the U-lock, and the BEM is applied to model the fluid domain and the layered soil. In deriving the system equations, the equilibrium and compatibility conditions at the fluid–structure, soil–structure, and the soil layer interfaces are used.

2. System description

The system consists of a fluid–contained structure embedded in layered soil deposits. Structures of this kind include hydraulic channels, locks, long storage tanks either open or covered by a flexible roof. One dimension of the structure is much longer than the other two with uniform loading so that the problem satisfies conditions of plane–strain, see Fig. 1. Also, the thickness of the walls is small compared to the width of the structure, which justifies application of thin plate theory. In order to consider the variation of soil properties along the depth, the half-space soil domain is divided into ‘n’ layers with different material properties. The system is subjected to harmonic seismic excitations described at the bedrock–soil layer interface.

The following sections describe the derivation of the equilibrium equation for each substructure, that is, the structure, the fluid, and the soil. The BEM is used to treat the soil and fluid domains, and the FEM is used to model the walls and bottom lining of the lock. Such an approach utilizes the advantages of each method. Specifically, BEM accounts for radiation damping automatically and restricts modeling of contact areas only, while the FEM is most suitable to model the finite size side and bottom walls of the lock [34].

The notation shown in Fig. 1 is adopted. The free surface of the fluid is denoted by ‘a’ and the structure–fluid interface is indicated by ‘b’. The top soil (1) layer has boundaries ‘e’, ‘c’, and ‘1’. The boundary ‘e’ is the free surface, boundary ‘c’ is the soil–structure interface, and boundary ‘1’ is the contact interface with layer (2). The bottom layer (n) has a top boundary ‘n − 1’ which is the contact interface with layer (n − 1) and bottom boundary ‘n’ which represents the interface with the half-space where the seismic excitation prescribed. A general layer (k) between the top layer and the bottom layer has top boundary ‘k − 1’ and bottom boundary ‘k′, where ‘k − 1’ is the contact interface between layers (k − 1) and (k).

3. BEM formulation and numerical treatment for the fluid and soil domains

3.1. BEM formulation for the fluid

For a compressible inviscid fluid with small displacements and zero initial conditions, the governing equation for the hydrodynamic pressure in excess of the hydrostatic pressure expressed in the frequency domain is the Helmholtz equation [35–37]:

\[ \Delta^2 P(\tilde{x}, \omega) + \kappa^2 P(\tilde{x}, \omega) = 0 \]  

(1)

where \( P(\tilde{x}, \omega) \) is the frequency response function for hydrodynamic pressure, \( \kappa = \omega/c \) is the wave number, \( c \) is the velocity of sound in the fluid, and \( \omega \) is the circular frequency of the excitation.

The corresponding boundary conditions are

\[ P(\tilde{x}, \omega) = p(\tilde{x}, \omega) \quad x \in \Gamma_1 \]  

(2)

\[ Q(\tilde{x}, \omega) = q(\tilde{x}, \omega) \quad x \in \Gamma_2 \]

where \( \Gamma_1 \) is the free surface boundary, and \( \Gamma_2 \) is the
contact interface, low case parameters $p$ and $q$ represent known values at the boundaries, and $Q$ is related to $P$ as given by

$$Q = \frac{\partial P}{\partial n}$$  \hspace{1cm} (3)

in which $\bar{n}$ is the outward normal to the fluid boundary.

The numerical solution of Eq. (1) together with the boundary conditions is obtained by applying the BEM. The starting integral equation of BEM for the fluid in the frequency domain is given by [38]

$$\delta(\vec{\xi})P(\vec{\xi}) = \int_{\Gamma} [Q(\vec{x})P(\vec{x}, \vec{\xi}; \kappa) - P(\vec{x})Q(\vec{x}, \vec{\xi}; \kappa)]d\Gamma'$$  \hspace{1cm} (4)

where $\delta(\vec{\xi})$ depends on the smoothness of boundaries, $P^*$ is the fundamental solution of Eq. (1) which is given by

$$P(\vec{x}, \vec{\xi}; \kappa) = \frac{1}{2\pi} K_0(ikr)$$  \hspace{1cm} (5)

$Q^*$ is the derivative of $P^*$ with respect to the outward normal, and $r$ is the distance between vectors $\vec{x}$ and $\vec{\xi}$. Dividing the boundary into $n$ elements and using constant boundary elements, see Fig. 2(a), a set of $n$ linear equations can be obtained [36,37]

$$[H][P] = [G][Q]$$  \hspace{1cm} (6)

where $[H]$, $[G]$ are $n \times n$ matrices and $[P]$, $[Q]$ are vectors of length $n$. A simplified form of Eq. (6) is given by

$$[D][Q] = [P]$$  \hspace{1cm} (7)

where $[D] = [H]^{-1}[G]$.

The degrees-of-freedom at the free surface in Eq. (6) can be condensed by employing the boundary conditions at the free surface of the fluid. At the free surface, if the effect of the surface waves is neglected, the boundary condition is

$$\{P_b\} = \{0\}$$  \hspace{1cm} (8)

If the waves at the free surface are considered, then $\{P_a\}$ is related to $\{Q_a\}$ by [12]

$$\{P_a\} = \frac{g}{\omega^2} \{Q_a\}$$  \hspace{1cm} (9)

where $g$ is the acceleration of gravity.

Eq. (7) can be rewritten for the boundaries ‘a’ and ‘b’ as [37]

$$\begin{bmatrix} D_{aa} & D_{ab} \\ D_{ba} & D_{bb} \end{bmatrix} \begin{bmatrix} \{Q_a\} \\ \{Q_b\} \end{bmatrix} = \begin{bmatrix} \{P_a\} \\ \{P_b\} \end{bmatrix}$$  \hspace{1cm} (10)

Substitution of the boundary condition of Eq. (9) into Eq. (10) yields

$$\begin{bmatrix} D_{aa} - \frac{g}{\omega^2} I_{aa} & D_{ab} \\ D_{ba} & D_{bb} \end{bmatrix} \begin{bmatrix} \{Q_a\} \\ \{Q_b\} \end{bmatrix} = \begin{bmatrix} 0 \\ \{P_b\} \end{bmatrix}$$  \hspace{1cm} (11)

From the first half of Eq. (11), $\{Q_a\}$ is related to $\{Q_b\}$ as given by

$$\{Q_a\} = -\left[\frac{g}{\omega^2} I_{aa} - D_{ab} \right]^{-1} \{D_{ab}\} \{P_b\}$$  \hspace{1cm} (12)

Substitution of the expression for $\{Q_b\}$ into the second half of Eq. (11) yields a condensed equation expressed in $\{P_b\}$ and $\{Q_b\}$ at the structure–fluid contact interface only, that is

$$[D']\{Q_b\} = \{P_b\}$$  \hspace{1cm} (13)

where

$$[D'] = [D_{bb}] - [D_{ba}] \left[\frac{g}{\omega^2} I_{aa} - D_{ab} \right]^{-1} [D_{ab}]$$  \hspace{1cm} (14)

In order to relate the variables $\{P_b\}$ and $\{Q_b\}$ of the fluid to the equilibrium equations for the soil and structure, that are expressed in terms of nodal forces and nodal displacements, use must be made of the boundary conditions at the structure–fluid contact interface, that is

$$q(\vec{x}, t) = p\vec{u}_i(\vec{x}, t)_{ba}(\vec{x}, t)$$  \hspace{1cm} (15)

and

$$\begin{bmatrix} \vec{i}'(\vec{x}, t) \\ \vec{j}'(\vec{x}, t) \end{bmatrix} = \begin{bmatrix} p\vec{u}_i(\vec{x}, t) \\ n_i \end{bmatrix}$$  \hspace{1cm} (16)

where $\vec{i}'$, $\vec{j}'$ are the components of the traction at the ith element, and $n_i$, $n_i'$ are the corresponding outwards normals [37], and $\vec{u}_i$ is the absolute acceleration of the structure.

From the boundary condition expressed by Eq. (15), $\{Q_b\}$ is related to $\{U_b\}$ in the frequency domain as given by

$$\{Q_b\} = \rho_i \omega^2 [C_b]\{U_b\}$$  \hspace{1cm} (17)

where

$$[C_b] = \begin{bmatrix} n_1 \cdots n_1 \\ \vdots \\ n_m \cdots n_m \end{bmatrix}$$  \hspace{1cm} (18)

in which $m$ denotes the total number of boundary elements at the structure–fluid contact area.

Similarly, based on the coupling condition of Eq. (16), $\{P_b\}$ is related to $\{T_b\}$ by

$$\{T_b\} = [C_b]^T \{P_b\}$$  \hspace{1cm} (19)

where

$$\{T_b\} = (T_X^1, T_Y^1, T_X^2, T_Y^2, ..., T_X^m, T_Y^m)^T$$  \hspace{1cm} (20)
Fig. 2. (a) Discretization of the lock–soil–fluid system: (1) fluid; (2) lock-lining; (3) soil interface; and (4) soil–bedrock interface. (b) Geometry of lock–soil–fluid system.
and
\[
\{P_b\} = \{P^1_b, P^i_b, P^2_b, P^3_b, \ldots , P^m_b\}^T
\]  
(21)

Also, the nodal force vector \(\{F_b\}\) is related to the tractions as given by
\[
\{F_b\} = [L_b]\{T_b\}
\]  
(22)

where
\[
\{F_b\} = \{F^1_b, F^i_b, F^2_b, F^3_b, \ldots , F^m_b\}^T
\]  
(23)

and
\[
[L_b] = \begin{pmatrix}
  l_1 & 0 & \ldots & \ldots & 0 \\
  0 & l_2 & \ldots & \ldots & 0 \\
  \ldots & \ldots & \ldots & \ldots & \ldots \\
  0 & 0 & \ldots & \ldots & l_m
\end{pmatrix}
\]  
(24)

in which \(l_i\) is the length of the \(i\)th boundary element.

In view of Eq. (19), Eq. (22) can be expressed as
\[
\{F_b\} = [L_b][C_b]^T\{P_b\}
\]  
(25)

Substituting the expression for \(\{Q_b\}\) from Eq. (17) into Eq. (13) and multiplying both sides of the resulting equation with \([L_b][C_b]^T\) yields the following relationship between the nodal forces and nodal displacements
\[
\{F_b\} = \rho_o \omega^2 [L_b][C_b]^T[D^f][C_b]\{U_b\}
\]  
(26)

Let
\[
[K_b] = \rho_o \omega^2 [L_b][C_b]^T[D^f][C_b]
\]  
(27)

Then Eq. (26) can be simplified to express the equilibrium equation for the fluid in terms of nodal displacements and forces, that is
\[
\{F_b\} = [K_b]\{U_b\}
\]  
(28)

BEM formulation for the soil

The governing equation for soil layers that are homogeneous, isotropic, and linearly elastic with small displacements is the well known Navier equation. Expressed in terms of transformed displacements \(U\) in the frequency domain, Navier’s equation is given by Eq. (29) where, for simplicity, zero initial conditions have been assumed; \(k = i\omega\), and \(c_1\) and \(c_2\) are the P- and S-wave velocities, respectively [39]
\[
(c_1^2 - c_2^2)U_{ij,ij} + c_2^2U_{ij,ii} - k^2U_j = 0
\]  
(29)

The corresponding boundary conditions to Eq. (29) are
\[
U_j(\bar{x}, k) = F_j(\bar{x}k) \quad \bar{x} \in \Gamma_1
\]  
(30)

\[
T_i(\bar{x}, k) = G_i(\bar{x}k) \quad \bar{x} \in \Gamma_2
\]  
(31)

where \(F(\bar{x}, k)\) and \(G(\bar{x}, k)\) are known displacements and tractions at the boundaries \(\Gamma_1\) and \(\Gamma_2\).

The BEM is employed to numerically solve Eq. (29) together with the boundary conditions expressed by Eq. (30). Similarly to Eq. (4), the starting expression for the BEM is the boundary integral equation
\[
\delta(\bar{x}, k)U_j(\bar{x}, k) + \int_{\Gamma} T_{ij}\text{d}\Gamma = \int_{\Gamma} U_{ij}^\prime T_{ij}\text{d}\Gamma
\]  
(31)

where the fundamental solutions: \(U_{ij}^\prime, T_{ij}\) are given by [34,38]
\[
U_{ij}^\prime(\bar{x}, \bar{x}, k) = \frac{1}{2\pi \rho c_2^2} (\Psi \delta_{ij} \chi_{x, x, j} T_{ij}^\prime(\bar{x}, \bar{x}, k))
\]  
(32)

\[
\chi = K_1 \left(\frac{kr}{c_2}\right) - \frac{c_2}{c_1} K_2 \left(\frac{kr}{c_1}\right)
\]  
(33)

\[
\Psi = K_0 \left(\frac{kr}{c_2}\right) + \frac{c_2}{kr} K_1 \left(\frac{kr}{c_2}\right) - \frac{c_2}{c_1} K_1 \left(\frac{kr}{c_1}\right)
\]  
(34)

in which \(K_0, K_1\) and \(K_2\) are modified Bessel functions of the second kind and order 0, 1, and 2, respectively.

Following well established discretization procedures for the boundaries and using constant boundary elements, see Fig. 2(a), Eq. (31) leads to a set of \(2N\) linear equations that relate the displacements to tractions, that is
\[
[H]\{U^i\} = [G]\{T^i\}
\]  
(35)

where \([H]\) and \([G]\) are \(2N \times 2N\) matrices, the \(2N\) vectors \([U^i]\) and \([T^i]\) are the displacement and traction vectors on the boundaries for the \(i\)th layer, and \(N\) is the number of boundary elements. A description of the methodology is given in several references, e.g. [36,37].

In order to derive the equilibrium equation for the whole system, the traction vector \([T^i]\) in Eq. (34) must be replaced by a nodal force vector. Specifically, Eq. (34) can be cast into the following form after some simple matrix manipulations:
\[
[K^i]\{U^i\} = \{F^i\}
\]  
(36)

where
\[
[K^i] = [L][G]^{-1}[H]
\]  
(37)

\[
[F^i] = [L]\{T^i\}
\]  
(38)
in which

\[ [L] = \text{diag}\{l_1 l_2 l_\cdots l_N l_N\} \]  

(38)

where \( l_i \) is the length of the \( i \)th boundary element.

4. FEM formulation for the lock and coupling of BEM with FEM

4.1. FEM formulation for the lock

The Mindlin–Kirchhoff plate theory [40,41] is utilized in the FEM formulation for the lock. According to this theory, the governing equations for bending and axial deformation are uncoupled. For a 2-D problem in the frequency domain, the governing equation for bending is reduced to the Bernoulli–Euler beam equation

\[
\frac{d^4}{dy^4} U_y - \lambda_1^2 U_y = 0
\]

(39)

where

\[
\lambda_1^2 = \frac{D_t h^3}{12(1 - \nu_t^2)}
\]

(40)

in which \( D_t \) is the flexural rigidity of the plate defined by

\[
D_t = \frac{E_t h^3}{12(1 - \nu_t^2)}
\]

(41)

where \( h \) represents the thickness of the plate, and \( \rho_t, E_t, \nu_t \) are the modulus of elasticity, mass density, and Poisson’s ratio of the plate, respectively. Notice that the bending stiffness \( EI \) in the classic Bernoulli–Euler beam theory for bending has been replaced by \( D_t \) to account for the longitudinal stiffness of the plate. The governing equation for axial deformation is given by

\[
\frac{d^2}{dx^2} U_x + \lambda_2^2 U_x = 0
\]

(42)

where

\[
\lambda_2 = \frac{\rho_t \sigma^2}{E_t/(1 - \nu_t^2)}
\]

(43)

The lock is divided into \( m \) elements, see Fig. 2(a). Following standard FEM procedures, the equilibrium equations for the axial and flexural response in the frequency domain can be written in the form [42,43]

\[
\begin{bmatrix}
D_{uu} & D_{u\theta} \\
D_{\theta u} & D_{\theta\theta}
\end{bmatrix}
\begin{bmatrix}
[U]^f \\
[\theta]
\end{bmatrix}
= \begin{bmatrix}
[F]^f \\
[M]
\end{bmatrix}
\]

(44)

where the subscripts \( u \) and \( \theta \) refer to nodal displacements and rotations, respectively and \( M \) denotes moments acting at the nodes. Through condensation of the rotational degrees-of-freedom, Eq. (44) can be rewritten in the following form [43]

\[
\]

(45)

where

\[
[K]^f = [D_{uu}] - [D_{u\theta}][D_{\theta\theta}]^{-1}[D_{\theta u}]
\]

(46)

4.2. Coupling of BEM with FEM

The governing equation for the whole system can be obtained by enforcing compatibility and equilibrium conditions at the soil–structure and structure–fluid interfaces. Specifically, at the interfaces the displacements from each substructure should satisfy the relationships

\[
\begin{align*}
\{U_e\} &= \{U_0^e\} \\
\{U_c\} &= \{U_0^c\} = \{U_0^e\} \\
\{U_b\} &= \{U_0^b\} = \{U_0^a\} = \{U_0^f\} \\
\{U_i\} &= \{U_i^{f-1}\} = \{U_i^f\} \\
\{U_g\} &= \{U_g^a\}
\end{align*}
\]

(47)

where the superscript \( s \) represents walls of the lock, \( f \) denotes fluid, and other superscripts indicate the location of a soil layer, subscripts denote the boundaries according to the adopted notation given earlier. The common displacements at the interfaces are indicated without superscripts, and \( U_g \) is the seismic excitation at the interface of the bedrock, see Fig. 1.

The forces from each substructure sum up to zero where no external forces are applied, that is

\[
\begin{align*}
\{F_0^e\} &= \{0\} \\
\{F_0^c\} + \{F_0^e\} &= \{0\} \\
\{F_0^b\} + \{F_0^a\} + \{F_0^f\} &= \{0\} \\
\{F_i^{f-1}\} + \{F_i^f\} &= \{0\}
\end{align*}
\]

(48)

Combining the equilibrium equations for each substructure and employing the compatibility conditions at the interfaces, the equilibrium equation for a system is obtained [37]

\[
[K][U] = \{P\}
\]

(49)

where

\[
\begin{align*}
\{U\} &= \{U_e, U_c, U_b, U_1, \ldots, U_{n-1}\}^T \\
\{F\} &= \{0, 0, 0, 0, \ldots, -K_{n-1,n}\}^TU_g
\end{align*}
\]

(50)

and

\[
\begin{align*}
\{P\} &= \{F_0^e, \ldots, F_{n-1}^e\}^T
\end{align*}
\]
5. Numerical example and parametric studies

The soil–structure system consists of a lock with a width 2B embedded in a soil layer with a depth H over a half-space bedrock (see Fig. 2(b)). The discretization of the three domains, i.e. water, lock and soil are shown in Fig. 2(a). The depth of the embedment is D, and it is assumed that the fluid fills up the lock. In the numerical examples, the contained fluid is water. The material properties of the lock are: mass density $\rho_f = 2500 \text{ kg/m}^3$, Poisson’s ratio $\nu_f = 0.3$, and damping ratio $\xi_f = 0.05$. The material properties of the soil are: modulus of elasticity $E_s = 100 \text{ MPa}$, mass density $\rho_s = 2000 \text{ kg/m}^3$, Poisson’s ratio $\nu_s = 0.33$, and damping ratio $\xi_s = 0.05$. To evaluate the effect of lock stiffness on the response, two cases, i.e. $E_f = 1 \times 10^3 \text{ MPa}$ and $E_f = 1 \times 10^6 \text{ MPa}$ are considered. Their relative stiffness is equal to 45 and 0.045, respectively. The relative stiffness and mass are defined by [44,45]

$$K_i = \frac{E_i h^3}{1 - \nu_i^2} \frac{E_i B^3}{1 + \nu_s}$$

$$M_i = \frac{\rho_f}{\rho_s}$$

(53)

(54)

(55)

Locks with relative stiffness of 500, 5, and 0.05 are characterized as rigid, intermediate, and very soft, respectively. Thus, locks with relative stiffness of $K_i = 45$ and 0.045 can be considered as stiff and soft, respectively. The ratio of lock width to thickness of the soil layer is $H/B = 2$. Two different embedment depths to width ratios $D/B = 1$ and $D/B = 2$, are considered to investigate the effects of embedment on the response. A horizontal harmonic excitation with amplitude $U_s$ and circular frequency $\omega$ is prescribed at the interface of the bedrock with the soil layer.

The results are presented in the form of relative displacements $U_i$, that is

$$U_i = \frac{U}{U_s}$$

(54)

where $U$ is the displacement at either the structure surface or the top free surface.

Two factors of great importance in the BEM formulation using fundamental solutions of the infinite soil domain are the truncation distance $L$ and the element size of the boundary elements $l_e$, see Fig. 2(b). To select optimum truncation distances and size of the boundary elements that maintain the balance between accuracy and efficiency for flexible foundations, a series of convergence studies has been conducted. For a detailed discussion, the reader is referred to the work by Xu [37]. The investigation in Ref. [37] arrived at the following general discretization guidelines for SSI analysis of systems subjected to seismic waves: the displacement response of the system can be divided into two different ranges, covering low and high frequency ranges with the fundamental frequency as the threshold. When the excitation frequencies are greater than the fundamental frequency, a sinusoidal-like curve that is referred to as ‘standing wave’ in the later discussion forms at the top free surface and vanishes after several circles. The convergence studies indicate that the required truncation distances should include four circles of standing waves, while the boundary element size should be one-tenth of the length of the standing wave. At the low frequency range, i.e. excitation frequencies lower than the fundamental frequency, the effect of discretization mesh is not so significant and larger element sizes as well as short truncation distances can be used.

Fig. 3(a)–(d) shows the relative displacements $U_i$ at the center of the bottom side of the locks versus the nondimensional frequency, $A_0$, defined by

$$A_0 = \frac{B \omega}{C_s}$$

(55)
As indicated in Fig. 3, solid lines represent relative displacements when no water is present, while dash-lines indicate relative displacement when the water is included. It is observed that the effect of water on the seismic response is not significant, especially at the low frequency range, see Fig. 3(a)–(c). However, as shown in Fig. 3(d), the relative displacements are considerably affected by the presence of water at the high frequency range for a flexible lock with $D/B = 2$. Also note that at a frequency equal to the fundamental frequency of the system, the displacements for all the four cases with water present are different from those with no water present. Specifically, the displacements with water in the lock are larger than those without the presence of water.
The effect of relative stiffness can be evaluated from Fig. 4(a) and (b) that shows the relative displacements $U_r$ at the center of the bottom side of water-filled locks. Fig. 4(a) shows the displacements $U_r$ for $D/B = 1$, and Fig. 4(b) depicts the displacements $U_r$ for $D/B = 2$. Comparison between Fig. 4(a) and (b) clearly demonstrates that the effect of lock stiffness is significant. Although at low frequencies, i.e. $A_0$ less than the fundamental frequency, both soft and stiff locks respond similarly, at high frequencies soft locks react very differently from stiff locks. Also, notice that within a certain frequency range, the relative displacements for soft locks are much larger than those for stiff locks, while at some other frequency range, the reverse is observed. Therefore, the presence of the water
does not always have a beneficial effect on the system response. When Fig. 4(a) is compared to Fig. 4(b), larger differences on the response are observed for the lock with deeper embedment. Therefore, it is reasonable to conclude that the effect of lock stiffness becomes more significant when the embedment of the lock increases.

The effect of embedment on the response of the fluid filled locks is investigated next. Fig. 5(a) and (b) show the relative displacements at the center of the bottom side of a soft lock and a stiff lock, respectively, for $D/B = 1$ and $D/B = 2$. As shown in Fig. 5, for both stiff and soft locks, an increase of embedment causes a decrease of the fundamental frequency of the system. It is also observed that an increase of embedment reduces the displacements around the fundamental frequency, but may result in larger displacements at a higher frequency. Finally, comparison between
Fig. 5(a) and (b) shows that the effect of lock embedment is more significant for soft locks than for stiff locks.

6. Conclusions

A study has been presented on the soil–structure–fluid interaction analysis of a lock system subjected to harmonic seismic waves. The water contained lock is embedded in soil layers supported by a half-space bedrock. The ground excitation is prescribed at the soil–bedrock interface. Through a hybrid BEM–FEM formulation, the flexible lock is modeled by the FEM, while the semi-infinite soil layers and the contained
References
